

Name: _____

Exam Style Questions



Sequences: Patterns

Corbettmaths

Ensure you have: Pencil, pen, ruler, protractor, pair of compasses and eraser

You may use tracing paper if needed

Guidance

1. Read each question carefully before you begin answering it.
2. Don't spend too long on one question.
3. Attempt every question.
4. Check your answers seem right.
5. Always show your workings

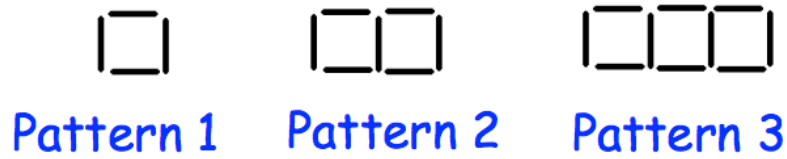
Revision for this topic

www.corbettmaths.com/contents

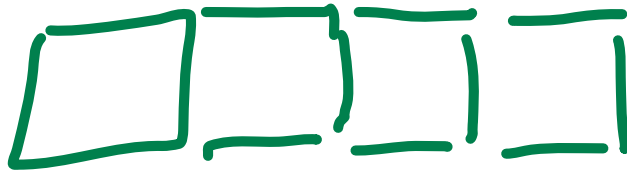
Video 290



1. These patterns are made of sticks



(a) Draw Pattern 4



(1)

(b) How many sticks will there be in Pattern 10?

$$4 + 3 + 3 + 3 \dots$$

$$4 + (10 - 1)3 = 4 + (9)(3) = 4 + 27 = 31$$

(1)

(c) Which pattern will use 40 sticks?

$$40 = 4 + (n - 1)3$$

$$40 = 4 + 3n - 3$$

$$40 = 1 + 3n$$

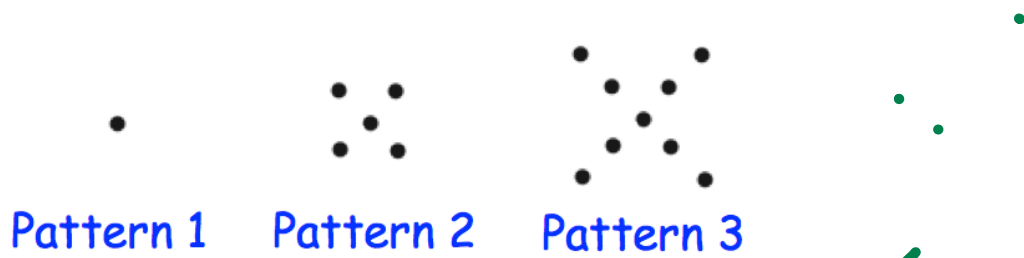
$$39 = 3n$$

$$13 = n$$

$$13$$

(1)

2. Here is a pattern of dots



(a) Continue the pattern to show Pattern 4



(2)

(b) How many dots will there be in Pattern 6?

$$1 + 4 + 4 + 4 \dots$$

$$1 + (6-1)4 = 1 + (5)(4)$$

$$= 1 + 20 \rightarrow 21$$

(1)

(c) Which pattern will use 77 dots?

$$77 = 1 + (n-1)4$$

$$77 = 1 + 4n - 4$$

$$77 = 4n - 3, \quad 80 = 4n \rightarrow 20$$

(1)

(d) Explain why there will **not** be a pattern that uses 200 dots.

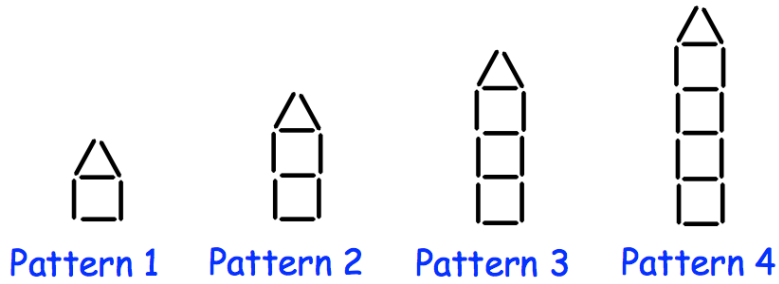
$$200 \text{ has to } = 4n - 3$$

so $203 \text{ has to be } 4n$ but 203 is

not even so not $n \times 4$ table

(1)

3. Patterns are made of sticks



(a) Complete the table for Pattern 4.

Pattern Number	1	2	3	4	5
Number of Sticks	6	9	12	15	18

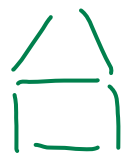
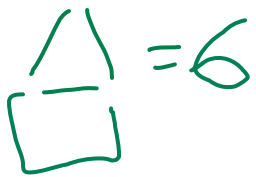
$+3$
 $+3$
 $+3$
 $+3$
(1)

(b) Sketch Pattern 5



(1)

(c) Which pattern will have 30 sticks?



etc

so

$$30 = 6 + (n-1)3$$

$$30 = 6 + 3n - 3$$

$$30 = 3 + 3n$$

$$10 = 1 + n$$

$$n = 9$$

(1)

(d) Here is the rule for working out the number of sticks

Multiply pattern number by 3 and add 3
 $n \quad \times 3 \quad + 3$

How many sticks will be in Pattern 200?

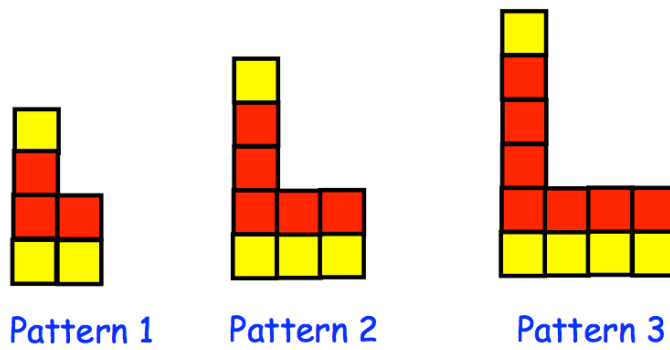
$n = 200$

so $200 \times 3 + 3$
 $= 600 + 3$

603

(1)

4. Here is a pattern of red and yellow squares.



(a) Here is a method for working out the number of red squares in each pattern.

Complete the method for Pattern 20.

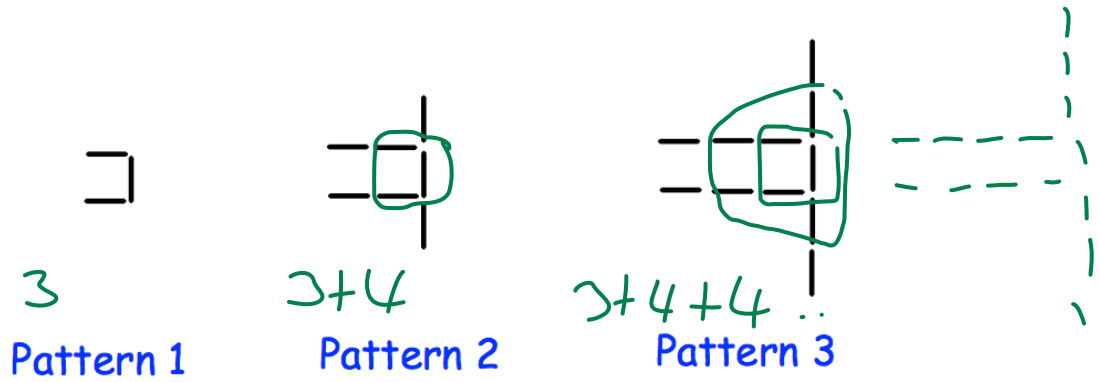
Pattern 1	$3 + 2 \times 0 = 3$	<i>mult first!</i>
Pattern 2	$3 + 2 \times 1 = 5$	
Pattern 3	$3 + 2 \times 2 = 7$	
Pattern 4	$3 + 2 \times 3 = 9$	
⋮		
Pattern 20	$3 + (2 \times 19) = 3 + 38 = 41$	(2)

(b) Which statements below are true?

- A**
Pattern 10 has 11 yellow squares
false — 2 more than the pattern
- B**
The number of red squares is always odd
True — even + odd
- C**
Every pattern has more red squares than yellow squares
False — pattern 1 doesn't!
- D**
Pattern 5 has 11 red squares
True

.....
(2)

5. These patterns are made from sticks.



(a) Draw Pattern 4

(1)

(b) How many sticks will there be in Pattern 5?

$$3+4+4+4 \dots$$

$$3+(5-1)4 = 3+20-4 = \underline{\quad 19 \quad}$$

(1)

(c) Write down a rule for continuing the patterns.

Keep adding 4

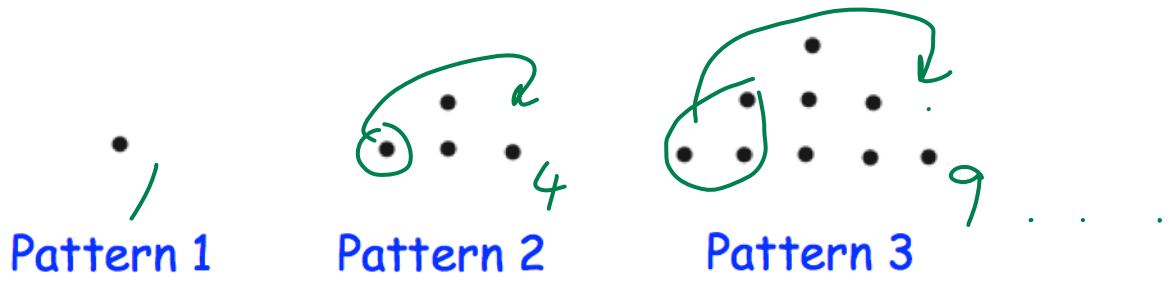
(1)

(d) Explain why you **cannot** make a pattern with exactly 44 sticks.

44 would have to be $3+(n-1)4$
 or $3+4n-4$, $4n-1$ $4n$ is same as $4 \times$ table
 44 is in the $4 \times$ table not one less

(1)

6. Dots are used to make a sequence of patterns.
The first three patterns are shown.

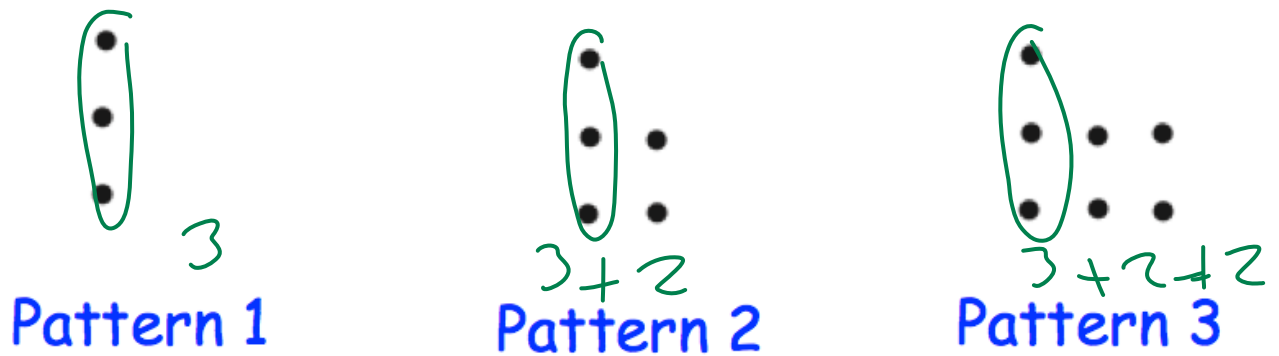


How many dots are needed to make Pattern 6?

$$\begin{array}{ccc}
 \begin{array}{c} \bullet \\ 1^2 \end{array} & & \begin{array}{c} \bullet \bullet \\ \bullet \\ 2^2 \end{array} \\
 & & \begin{array}{c} \bullet \bullet \\ \bullet \bullet \\ \bullet \\ 3^2 \end{array} \\
 6^{\text{th}} \text{ pattern is } 6^2 & = & 36 \text{ dots}
 \end{array}$$

$$\begin{array}{r}
 36 \\
 \hline
 (2)
 \end{array}$$

7. Here are some patterns made from dots.



(a) Complete the table for Pattern 4.

Pattern Number	1	2	3	4
Number of dots	3	5	7	9 ✓

$\xrightarrow{+2}$ $\xrightarrow{+2}$ $\xrightarrow{+2}$

(1)

Harry wants to find the number of dots in Pattern number 50.

(b) Write down a method he could use.

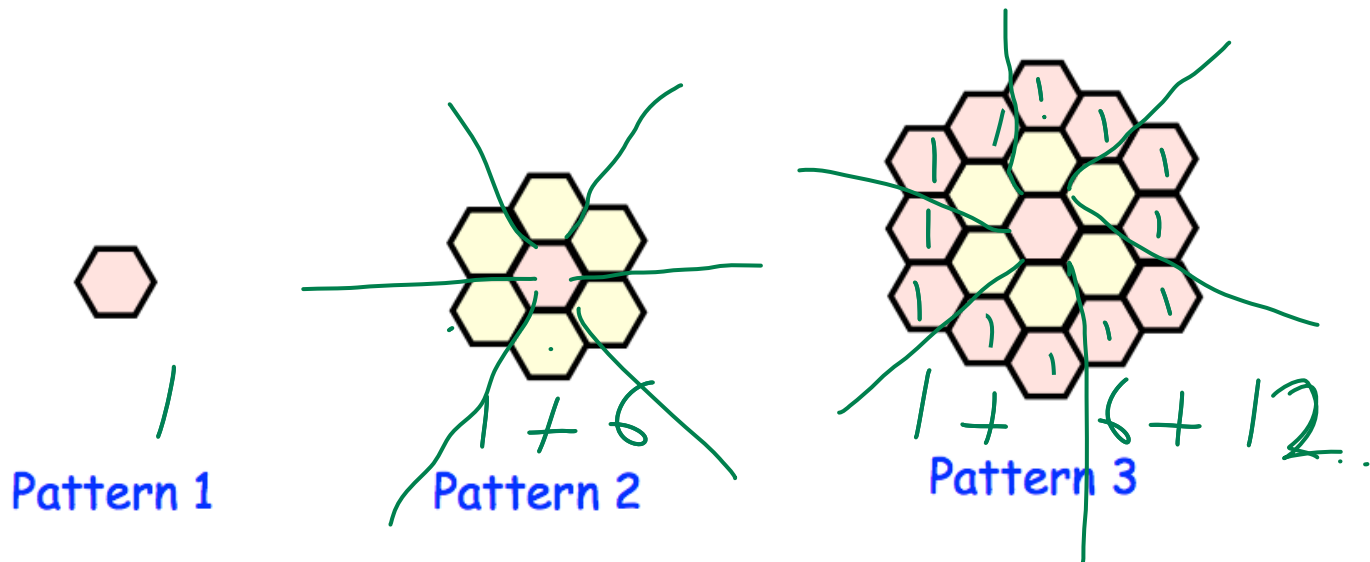
$$3 + (50 - 1) \times 2$$

(1)

8. Here is a tile.



Here is a sequence of patterns made from these tiles.



How many of these tiles are needed to make Pattern number 6?

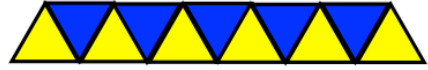
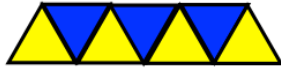
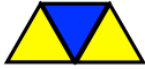
$1 + 6 \times 1$ then 6×2
then 6×3 . . .

$$\begin{aligned} \text{So } & 1 + 6 + 12 + 18 + 24 + 30 \\ & = 1 + 15(6) \\ & = 1 + 90 \end{aligned}$$

91⁽³⁾

9. Patterns are made from yellow and blue triangles.

$y = \text{yellow}$



Pattern 1

$y = 2$

Pattern 2

$y = 4$

Pattern 3

$y = 6$

(a) How many yellow triangles are there in the n th pattern?

Pattern $N^{\circ} \times 2 = \text{Triangles}$

$$T = 2n$$

(2)

(b) How many blue triangles are there in the n th pattern?

Blue = 1, 3, 5, ... $(P \times 2) - 1 = \text{Triangles}$

P	1	2	3	n
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$$T = 2n - 1$$

(2)

(c) How many triangles, yellow and blue, are there in the 100th pattern?

Add both formulas

So $(T = 2n) + (T = 2n - 1)$

399 ✓

(2)

When $n = 100$

$$T = 2(100) + T = 2(100) - 1$$

$$= 200 + = 199$$

$$= 399$$