

$\pi$  future: maThs  $\pi$   
infinite: infinite

$\pi$  maThs E1 E2 E3  $\pi$

$\pi$  maThs Level 1 & 2  $\pi$



# Equivalences

# Course Content: Choose your topic ...

MATHS L1 to L2

## Whole Number and Functions



place value



negative numbers



add and subtract



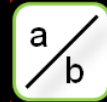
multiply divide



round numbers



ratio scale



fraction



decimal numbers

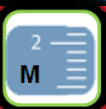


percent



percent decimal fraction

## Parts of a whole



metric measure



imperial measure



perimeter



area



volume



formulae bodmas

## Measure and Shape



charts data



averages



probability

## Handling Data

## Topic Introduction : Equivalents



Percent/Decimal  
Fraction Equivalents

When you have studied the topics of Percentage, Decimal and Fractions it is important to realise that all three of these topics are connected and really just show the same value in different ways.

If you get good at changing between the three number systems for parts of a whole you will be able to select the quickest and easiest methods for solving lots of problems and calculations.

This topic is especially useful in the topic of pie charts where different slices of a chart can be shown using different values so check this topic out too after this one!

Choose an icon to select where to start





## Warm up Exercise 2



Percent



N=480  
%= 24

Do-talk-record

A

L2/L1

L2. 24% of 480 is?

- a)  $N \times 100 \div 24$  because.....
- b)  $N \times 0.24$  because.....
- c)  $N \times 6/25$  because.....
- a)  $N \times \% \div 100$  because.....

L1. 24% of 480 is?

- A) is  $1/24$  because.....
- B) is approximately  $1/4$  because.....
- C) is approximately 120 because....
- D) is  $0.24 \times 480$  because.....



## Warm up Exercise 3



Fractions

Do-talk-record

C

L2/L1



L2. 14% is .... $1/7$ ?

- a)  $>$  because.....
- b)  $<$  because.....
- c)  $\approx$  because.....
- d)  $=$  because.....

L1. 8% is ...  $1/12$ ?

- A)  $>$  because.....
- B)  $<$  because.....
- C)  $=0.8$  because.....
- D)  $=0.08$  because.....



## Warm up Exercise 4



Fractions

Do-talk-record

B

L2/L1



L2. 36% of 500 is the same as?

- a) 180% of 100 because.....
- b) 1.8% of 1000 because.....
- c) 18% of 1000 because.....
- d) 72% of 250 because.....

L1. 10% of 750 is the same as?

- A) 100% of 75 because.....
- B) 20% of 1500 because.....
- C) 20% of 375 because.....
- D) 50% of 150 because.....

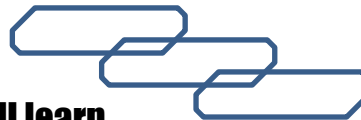


# Progress Checker 1

What do you already know about Equivalences between % / Decimals / Fractions ?

How would you rate your skills in changing between the three systems ?

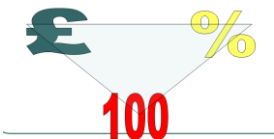
- 1) Excellent ability
- 2) Good ability, but working to improve
- 3) Ok, making a start but I know I have lots to still learn



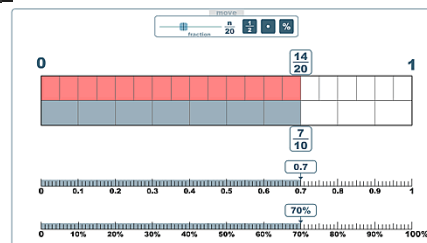
My aims for today  are...

- A Recognise that the three systems for parts of a whole are the same thing written differently
- B Change one system to another, eg.. change fractions to decimals
- C Use appropriate systems to solve and simplify problems

Remember how to convert!!



A grid with three columns labeled F, D, and P. In the F column, there is a pie chart with 1/3 shaded purple and the fraction  $\frac{1}{3}$ . In the D column, there is the decimal 0.33. In the P column, there is the percentage 33.3%. Below these, there are three input fields: a fraction field with  $\frac{1}{3}$ , a decimal field with 0.33, and a percentage field with 33.3%.



Decimal	Percent	Fraction
1	100%	1/1
0.75	75%	3/4
0.50	50%	1/2
0.25	25%	1/4
0.33	33%	1/3
0.20	20%	1/5
0.10	10%	1/10
0.01	1%	1/100





## Introductory Video and Discussion

**Is it better to stick with one method or change between systems during a calculation ?**

**Can all fractions be changed exactly to decimals ?**

**How are decimals and percentages different ?**

**When might we want to change between decimals / % / fractions ?**

**Which is the best system from counting values between 0 and 1 ?**

**Which is the newest system of counting parts of a whole ?**



**Watch the introductory video and then discuss the above**

**Your thoughts..**



# Vocabulary and Jobs

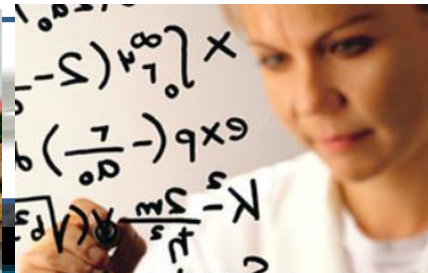
- Equivalent**
- Decimal**
- Fraction**
- Percentage**
- Change**
- Convert**
- Conversion Triangle**
- Decimal places dps**
- Simplify**
- Ratio**
- Alter**
- Reduce**

These are the words you will be using in this topic

- Hotel Management
- Government Statistics
- Scientist
- Mathematician
- Engineer
- Health Care
- Media
- Cooking
- Manufacturing

Statist.... Can you think of more?

.....  
.....

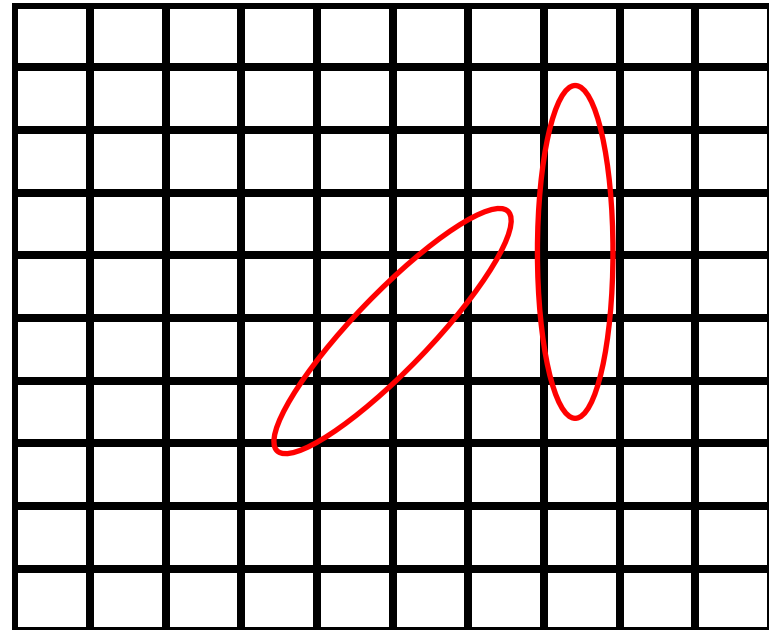
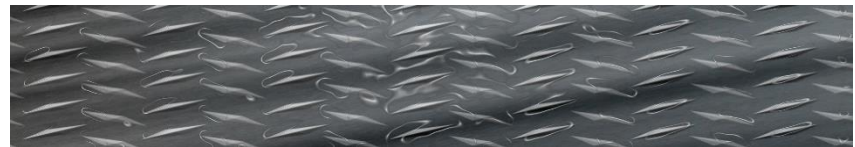




## Lesson: Concept Activity

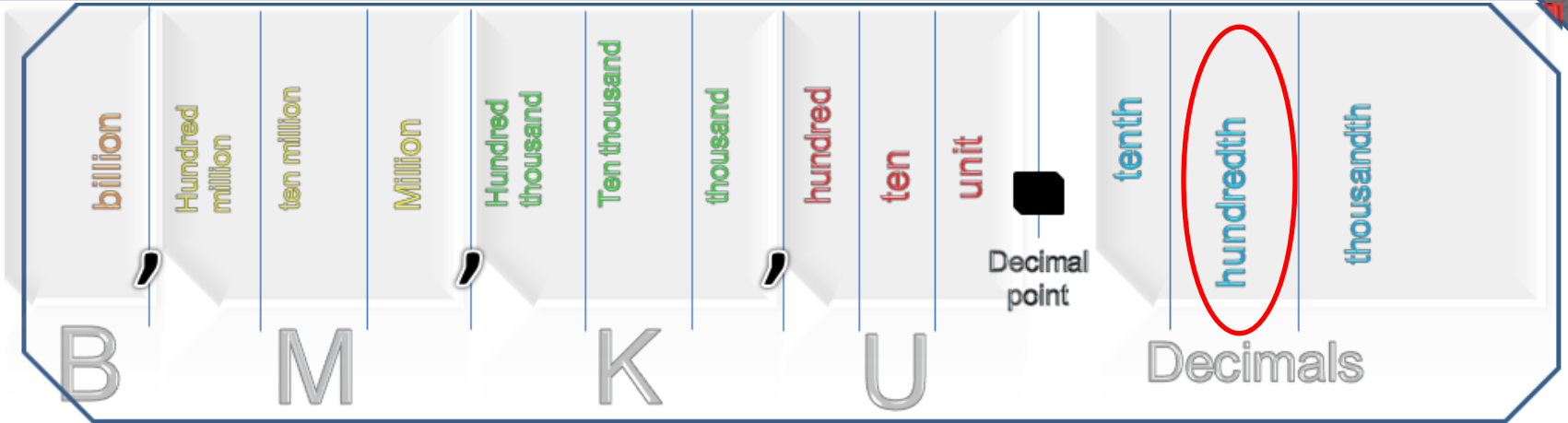
### *Four in a row equivalences grid*

- **Pair up**
- **Choose a square to start**
- **Write in it the % of the grid it is**
- **Next player chooses another square**
- **Write the fraction out of 100 that square is**
- **First player now chooses a second square and writes the decimal that square is**
- **Alternate between players choosing squares and writing the % -- fract – decimal values until one player has 4 squares in a line in any direction**





# Lesson: Main Teach 1



To be able to convert between the three systems of counting parts of a whole that have been invented over many centuries, first 'FRACTIONS' (5000 years old), then 'DECIMALS' (200 years old) and finally 'PERCENTAGES' (60 years old), you need to know your place values, especially the H U N D R E D T H S.

One cut into a hundred is also .....  $1/100$ ..... one hundredth.....one percent..... 0.01

So ...if we put a 7 in the hundredths column to show we have seven parts out of the whole amount (such as 7p out of a £1) how could we show this value???

Well... 7 out of a hundred is .....  $7/100$  .....seven hundredths.....seven percent..... 0.07



1.

To change a decimal to a percent we multiply by 100 or move the decimal point two places to the right.

$$0.30 = 30\%$$

2.

To change a percent to a decimal we divide by 100 or move the decimal point two places to the left.

$$45\% = 0.45$$

3.

To change a percent to a fraction we place it on top of 100.

We then simplify it if we can.

$$56\% = 56/100$$

4

To change a decimal to a fraction we turn it to a percent and place it on top of 100.

$$0.95 = 95\% = 95/100$$

5.

To change a fraction to a percent we divide the denominator into 100 and multiply by the numerator

$$3/5 = 60/100 = 60\%$$

6.

To change a fraction to a decimal we divide the numerator of the fraction by the denominator

$$6/7 = 0.857..$$

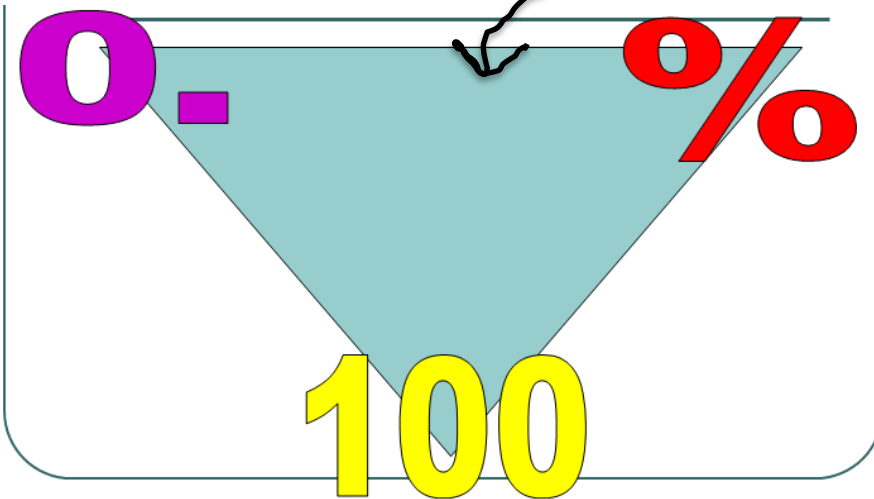


# Lesson: Main Teach 4

There are some basic equivalents that you can learn off by heart that are really useful in simplifying and speeding up your calculations.

Try to learn the basic equivalents in the grid opposite 

There is also a neat upside down triangle that can help you to convert any %/frac/dec number. Just write the value out of 100 in the space at the top of the triangle .... Cover up the two systems you don't want to see to leave the one you want ..... Here, try **73** ... put it here.... what did you get?? ..... Hopefully 73% or 73/100 or 0.73 ..great !!



Decimal	Percent	Fraction
1	100%	1/1
0.75	75%	3/4
0.50	50%	1/2
0.25	25%	1/4
0.33	33%	1/3
0.20	20%	1/5
0.10	10%	1/10
0.01	1%	1/100



## Lesson: Try out

### Block 1 : Watch tutor led demo (in class or on video)

- Try these,
- |  |  |
|--|--|
| 1) Which is larger $\frac{1}{2}$ or 0.75 | 2) Which is smaller $\frac{3}{4}$ or 0.25              |
| 3) Which is larger $\frac{2}{10}$ or 0.7 | 4) Which is smaller 40% or 0.35                        |
| 5) Which is larger 25% or 0.6            | 6) Convert $\frac{1}{2}$ into decimals and percentages |

### Block 2 : Watch tutor led demo (in class or on video)

- Try these,
- |  |   |
|--|---|
| 7) Convert 0.23 into fractions           | 8) Change $\frac{15}{100}$ into percentage                        |
| 9) Make $\frac{79}{1000}$ into a decimal | 10) Convert 0.05 into the simplest fraction                       |
| 11) Alter 63% to be a decimal            | 12) Add together $\frac{3}{10} + 0.27$ writing your answer as a % |

### Block 3 : Watch tutor led demo (in class or on video)

## Level Two

- Try these,
- |   |   |
|---|---|
| 13) Change 0.047 into a fraction        | 14) Convert $\frac{116}{1000}$ into a decimal |
| 15) Write 16.9% as a fraction           | 16) Write 0.437800..... as a fraction         |
| 17) $\frac{241}{10000}$ is ..... as a % | 18) Make 0.2% into a decimal                  |



## Lesson: Websites and links

**Website on converting between %, decimals and fractions**

<http://www.mathsisfun.com/decimal-fraction-percentage.html>

**Conversion tool on website for you to check your answers**

<http://www.purplemath.com/modules/percents.htm>

**3 number lines to match %/frac/decimals to**

<http://www.ictgames.com/equivalence.html>

**Card matching game**

[http://www.mathplayground.com/matching\\_fraction\\_percent.html](http://www.mathplayground.com/matching_fraction_percent.html)

**Another card matching game**

<http://nrich.maths.org/1249>

**An online converter between fractions and decimals (with hundredths also)**

<http://www.amblesideprimary.com/ambleweb/mentalmaths/fracto.html>



## Lesson: Activity E

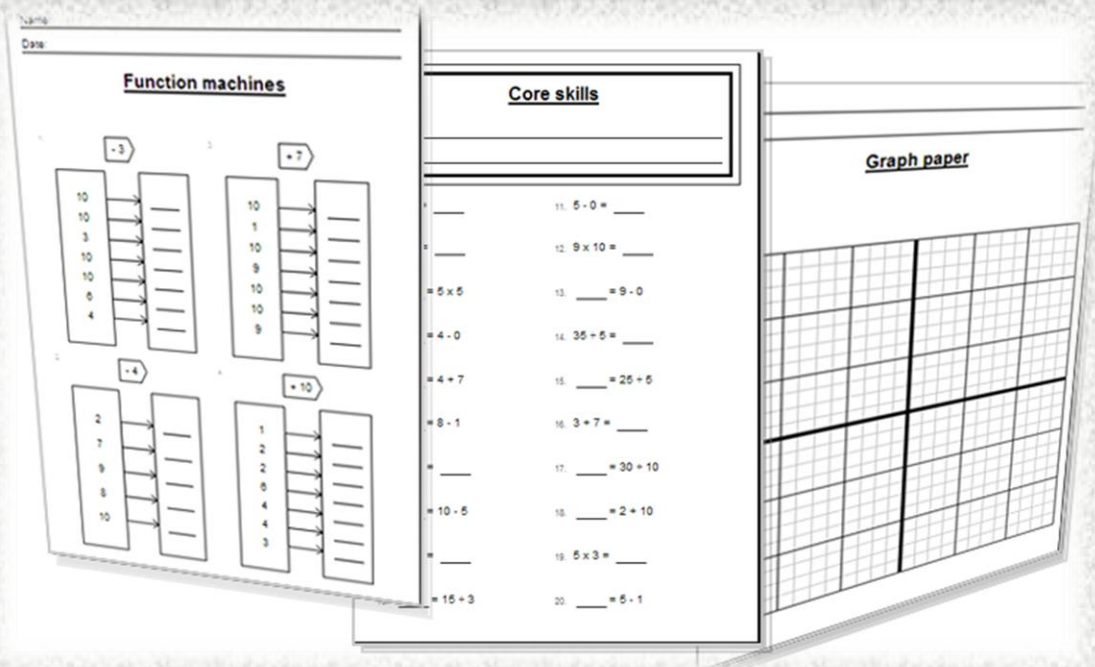
Try a variety of written practice

**Worksheets**

**Workbooks**

**Practice Exam Papers**

**Maths Problems**





## Lesson: Practice – just the numbers

### Convert Decimals to Percent

- 1)  $0.40 = \dots\dots\dots\%$
- 2)  $0.75 =$
- 3)  $0.16 =$
- 4)  $0.62 =$
- 5)  $0.04 =$
- 6)  $0.005 =$
- 7)  $0.806 =$
- 8)  $0.999 =$
- 9)  $0.47231 =$

Level Two

### Convert Percent to Decimals

- 10)  $15\% = 0. \dots\dots ?$
- 11)  $48\% =$
- 12)  $82\% =$
- 13)  $6\% =$
- 14)  $0.5\% =$
- 15)  $1.2\% =$
- 16)  $16.9\% =$
- 17)  $22.5\% =$

### Convert Decimals to Fractions

- 18)  $0.23$
- 19)  $0.18$
- 20)  $0.98$
- 21)  $0.33$
- 22)  $0.08$
- 23)  $0.005$
- 24)  $0.612$
- 25)  $0.8954$
- 26)  $0.4032$

### Convert Fractions to Decimals

- 27)  $1/5$
- 28)  $3/10$
- 29)  $92/100$
- 30)  $25/75$
- 31)  $16/25$
- 32)  $1/3$
- 33)  $18/26$
- 34)  $2040/3928$

### Convert Fractions to Percent

- 35)  $4/5$
- 36)  $9/10$
- 37)  $83/100$
- 38)  $1/6$
- 39)  $8/9$
- 40)  $900/1000$
- 41)  $23/49$
- 42)  $6/80$
- 43)  $2M / 18M$

### Convert Percent to Fractions

- 44)  $1\%$
- 45)  $20\%$
- 46)  $85\%$
- 47)  $72\%$
- 48)  $16\%$
- 49)  $9\%$
- 50)  $0.7\%$
- 51)  $11.8\%$



## Lesson: Practice – word problems

- 1) I scored 15 out of 20 question correct. What was my percentage score?
- 2) A train journey is 45% of the way through. How many of the 50km has the train journey completed so far?
- 3) A charity has collected £0.381 M. Its target is a million pounds. What percentage of the money has still to be collected?  
**Level Two**
- 4) A bus fare goes up £0.15 and was originally £1.20. What was the percentage increase? (hint, write as a fraction first then convert)  
**Level Two**
- 5) Mike spends 45% of his day sleeping. What fraction of 24 hours is this?  
**Level Two**
- 6) A computer readout shows a dial setting to be at 0.35852..... . The dial should be set on setting 3 out of 5. Is the computer readout correct to the dial setting?



## TOPIC ANSWERS 1

### Just the numbers

- 1) 40%
- 2) 75%
- 3) 16%
- 4) 62%
- 5) 4%
- 6) 0.5%
- 7) 80.6%
- 8) 99.9%
- 9) 47.231%

### Just the numbers

- 18) 23/100
- 19) 18/100 or 9/50
- 20) 98/100 or 49/50
- 21) 33/100 (about 1/3)
- 22) 8/100 or 2/25
- 23) 5/1000 or 1/200
- 24) 612/1000
- 25) 8954/10,000
- 26) 4032/10,000

### Just the numbers

- 35) 80%
- 36) 90%
- 37) 83%
- 38) 16%
- 39) 89%
- 40) 90%
- 41) 47%
- 42) 7.5%
- 43) 11%

- 10) 0.15
- 11) 0.48
- 12) 0.82
- 13) 0.06
- 14) 0.005
- 15) 0.012
- 16) 0.169
- 17) 0.225

- 27) 0.2
- 28) 0.3
- 29) 0.92
- 30) 0.333...
- 31) 0.64
- 32) 0.333...
- 33) 0.69...
- 34) 0.519...

- 44) 1/100
- 45) 20/100 or 1/5
- 46) 85/100
- 47) 72/100
- 48) 16/100
- 49) 9/100
- 50) 7/1000
- 51) 118/1000

### Word Problem ANSWERS

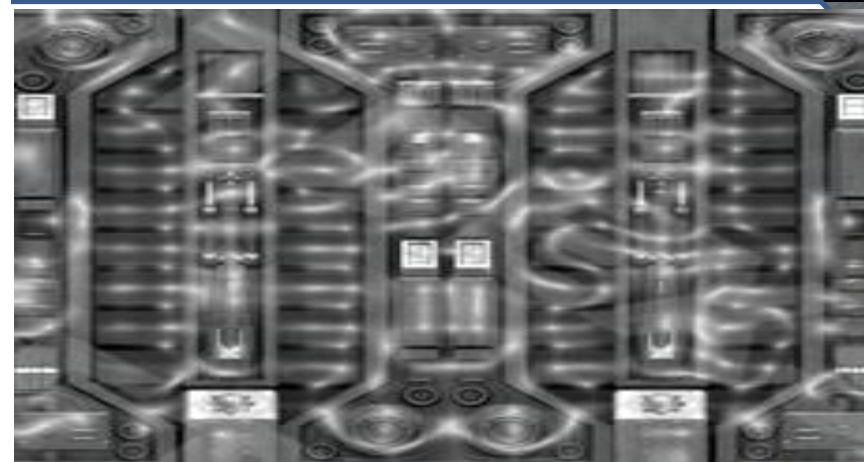
- 1) 75%
- 2) 22.5 km
- 3) 61.9%
- 4) 12.5%
- 5) 10.8 hours
- 6) No, the readout should say 0.8



## TOPIC ANSWERS 2 Fuctional Skills Activity

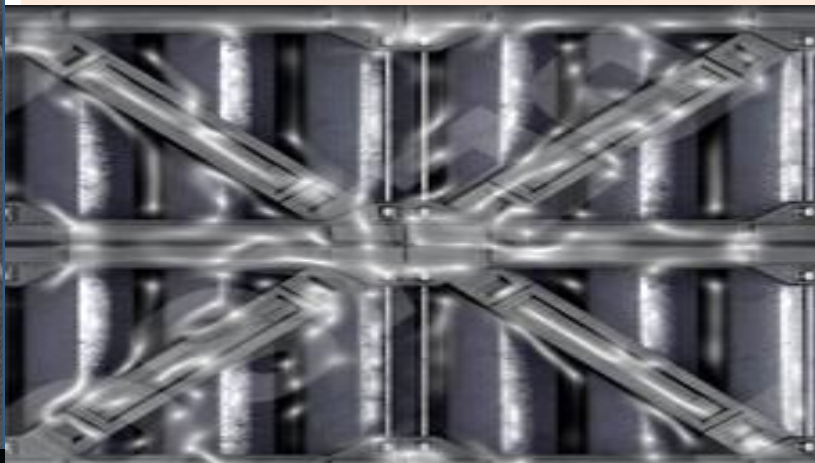
### Answers

- 1a)  $0.2 = 20\%$     $0.166 = 16.6\%$     $0.05 = 5\%$   
•      $0.15 = 15\%$     $0.25 = 25\%$     $0.6 = 60\%$
- b)  $2/5 = 40\%$     $1/8 = 12.5\%$     $6/30 = 20\%$   
•      $11/44 = 25\%$     $6/20 = 30\%$     $8/20 = 40\%$   
•      $3/20 = 15\%$
- c) 5%, 12.5%, 15%, 16.6%, 20%, 25%, 33.3%, 30%, 40%, 60%, 66.7%
- d) 15%, 20%, 25%, 40%



### Answers

- 2 a)  $16.6\% = 1/6$     $12.5\% = 1/8$     $33.3\% = 1/3$     $66.7\% = 2/3$
- b) Choose 4 discount totals listed in fractions and percentages from 5%, 15%, 20%, 25%, 30%, 40%, 60%,  $1/3$ ,  $2/3$ ,  $1/6$  and  $1/8$ .
- c) Explain the 4 choices. Have you considered the easiest for customers to understand, or the range of discounts you think should be available?



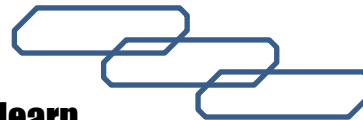


# Progress Checker 2

**What do you now know about Equivalences between % / Decimals / Fractions ?**

**How would you now rate your skills in changing between the three systems ?**

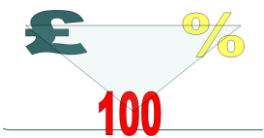
- 1) Excellent ability
- 2) Good ability, but still working to improve
- 3) Ok, made a start but I know I have lots to still learn



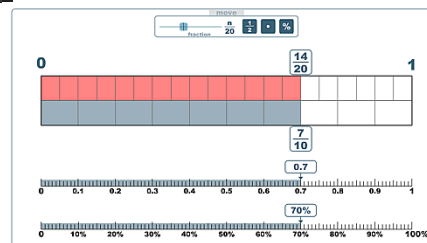
**My aims for today**  **were...**

- A Recognise that the three systems for parts of a whole are the same thing written differently**
- B Change one system to another, eg.. change fractions to decimals**
- C Use appropriate systems to solve and simplify problems**

Remember how to convert!!



F	D	P
$\frac{1}{3}$	$0.3\bar{3}$	$33.\bar{3}\%$



Fraction	Percent	Decimal
1	100%	1/1
0.75	75%	3/4
0.50	50%	1/2
0.25	25%	1/4
0.33	33%	1/3
0.20	20%	1/5
0.10	10%	1/10
0.01	1%	1/100





## Continuing to Study and Learn

**What else can you do to help yourself to learn and practice? Here are ten suggestions, record which you do each week and also record your progress.**

**Internet websites**

**Repeat the lesson, make notes, organise a folder, revise**

**Own maths workbook**

**Study together with a friend or family member**

**Finish activities in this book**

**Complete class handouts or tasks**

**Practice exams / past papers**

**Use maths skills learnt at home or at work in real situations**

**Play games**

**Experiment yourself, try new things ask yourself questions**



**Try making a graph of number of practice methods you use against your progress score in each topic. Are you showing more practice gives better results?**